Diffractive Imaging of Conical Intersections Amplified by Resonant Infrared Fields

Daniel Keefer, Jérémy R. Rouxel, Flavia Aleotti, Francesco Segatta, Marco Garavelli, and Shaul Mukamel

ABSTRACT: The fate of virtually all photochemical reactions is determined by conical intersections. These are energetically degenerate regions of molecular potential energy surfaces that strongly couple electronic states, thereby enabling fast relaxation channels. Their direct spectroscopic detection relies on weak features that are often buried beneath stronger, less interesting contributions. For azobenzene photoisomerization, a textbook photochemical reaction, we demonstrate how a resonant infrared field can be employed during the conical intersection passage to significantly enhance its coherence signatures in time-resolved X-ray diffraction while leaving the product yield intact. This transition-state amplification holds promise to bring signals of conical intersections above the detection threshold.

INTRODUCTION

Recent advances in X-ray light sources, especially at free-electron lasers (FELs), offer novel windows into molecular dynamics. A particularly powerful technique is time-resolved X-ray diffraction (XRD). Traditionally used for structure determination in stationary molecular samples, the peak brilliance of X-rays has consistently been increased to allow for smaller and smaller crystal sizes. Once the goal of pushing XRD to the single molecule limit is achieved, direct imaging of ultrafast photochemistry will be possible.

X-ray photons scatter off the electronic charge density. Since molecules undergoing a photochemical transformation are in a nonstationary superposition of electronic and vibrational states, there are many overlapping contributions to the diffraction pattern. Disentangling them is necessary to unravel the mechanism of a photochemical process. This could mean maximizing the scattering from the excited-state electron density, allowing the structure determination of individual electronic states.

The direct imaging of conical intersections (CoIns) is an even more intriguing possibility. These are regions in the molecular landscape where electronic states are very close in energy and thus strongly coupled to nuclear motions that occur on a similar time scale. A series of pioneering ultrafast pump–probe spectroscopic experiments in the past has induced a paradigm shift in our understanding of photochemical reactions. A sudden change in absorption features is observed on the femtosecond (1 fs = 10−15 s) time scale once the molecule relaxes from one electronic state to another. CoIns are now widely recognized as the decisive events in ultrafast molecular transformations such as the primary event of vision. They occur in every polyatomic molecule and promote radiationless transitions between excited states. The energy, topology, abundance and accessibility of CoIns, and what quantum pathways they connect, thus determine the fate of photochemical processes. Once a nuclear wavepacket, initially located in one electronic state, reaches the CoIn, it branches and partly relaxes to other electronic states. A vibronic coherence characterized by the overlap of the nuclear wavepackets at two surfaces then emerges and persists for a short amount of time. This unique spectroscopic signature of the CoIn is generally much weaker than that of the state populations and is hard to detect.

In the XRD signal, coherences contribute by combined elastic/inelastic photon scattering from the electronic transition density. Once isolated, this term could provide a spatial image of the CoIn and thus direct insight into the determining events of molecular photochemistry. A major difficulty is that the coherence magnitude is much weaker compared to elastic scattering from electronic states, and thus, it is buried in the total signal.

In this simulation study, we show how to significantly enhance the coherence signal and thereby offer a potential
solution to this problem. The time-resolved diffraction patterns for the textbook cis → trans photoisomerization of azobenzene involving a CoIn passage are simulated. An infrared (IR) laser field resonant with the electronic transition in the CoIn region is employed. By slightly shifting around populations between the excited states the coherence is significantly enhanced while leaving the natural photochemistry virtually intact.

Previous studies that employed coherent infrared (IR) light fields at CoIns have aimed at controlling the photochemistry by playing with the carrier-envelope phase of the pulse\textsuperscript{15,16} or by altering the CoIn topology through the dynamic Stark effect and thus influencing the photochemical outcome.\textsuperscript{17} Here, rather than controlling the photochemistry, we focus on noninvasive amplification for spectroscopy and imaging. Our approach demonstrates a novel utilization of IR laser pulses at CoIns that can enable transition-state imaging in analogy to Zewail’s transition state spectroscopy.\textsuperscript{18} Optimal control theory (OCT)\textsuperscript{19,20} is employed to optimize laser pulses for coherence maximization. To record a holistic imaging of molecular photochemistry, OCT is also employed to maximize other contributions in the ultrafast XRD signal, allowing for, e.g., selective structure determination of excited states.

![DIFFRACTION SIGNAL OF AZOBENZENE PHOTOISOMERIZATION](https://doi.org/10.1021/jacs.1c06068)

Being switchable between both isomers with a high quantum yield,\textsuperscript{21–23} azobenzene has found numerous applications in fields like material science,\textsuperscript{24} photopharmacology,\textsuperscript{25} or optogenetics.\textsuperscript{26} Besides its practical relevance, the photochemical mechanism applies to many other molecules, giving our proposed scheme broad relevance.

An effective Hamiltonian with two nuclear degrees of freedom for nuclear wavepacket simulations of azobenzene cis → trans isomerization has been introduced recently.\textsuperscript{4,27} The first coordinate is the CNNC torsion angle between the two central nitrogens and the connected carbon atoms, connecting the cis geometry at $\text{CNNC} = 0^\circ$ and the trans at $\text{CNNC} = 180^\circ$. The second coordinate is the CNN bending angle between the two nitrogen atoms and one adjacent carbon atom, while the other CNN angle remains fixed. Initially, both CNN angles are at $116^\circ$ for the cis structure, and symmetry breaking is necessary to reach the minimum energy CoIn around $\text{CNNC} = 94^\circ$. High-level CASPT2 excited-state quantum-chemical calculations in this two-dimensional space were performed to obtain the potential energy surfaces (PESs) depicted in Figure 1.\textsuperscript{27}
Two-mode models with two or more states have a long history of success in the simulation of ultrafast nonadiabatic dynamics and interpretation of corresponding experiments. Two widely recognized examples are the pyrazine photo-reaction model of Domcke and co-workers\textsuperscript{28} and the rhodopsin model of Hahn and Stock.\textsuperscript{29} The latter is especially close related to azobenzene, as it describes a photoisomerization involving a torsion and a bending angle. Its validity is corroborated by repeated applications to date.\textsuperscript{30} Even from experimental data, two-mode models were concluded to adequately describe reactive torsional dynamics, like in the case of molecular motors.\textsuperscript{31} More general two-mode models are commonly used to simulate and describe fundamental effects of CoIn dynamics\textsuperscript{32,33} since a minimum of two modes is required to form a CoIn. The concept of reactive coordinates in general has been put forward for the photochemical reaction ring opening of cyclohexadiene (another textbook photochemical process) reproducing experimental data.\textsuperscript{34} This is in general justified for ultrafast reactions since within these time scales, upon photoexcitation, the molecular motion is coherently funneled into the reactive pathways. At later times (typically after a few hundred femtoseconds), internal vibrational relaxation to other modes takes place, not being captured by such Hamiltonians. Many more nuclear modes (up to few tens) can be treated by the multiconfigurational time-dependent Hartree (MCTDH) method,\textsuperscript{35} being a more approximate approach to nuclear quantum dynamics and showing broad success.

In our effective Hamiltonian for azobenzene photoisomerization, two electronic states, the ground state S\textsubscript{0} and the first excited state S\textsubscript{1} that has π* character, contribute to the process. The PESs are depicted in Figure 1B, with the CoIn region marked in black and the nuclear wavepacket drawn in red.

Initially, the wavepacket is located in the cis minimum of S\textsubscript{0}. Upon electronic excitation, the wavepacket mostly is located in S\textsubscript{1}, thanks to a nonvanishing transition dipole moment between the two states. It first evolves to larger CNN angles and then moves predominantly along the reactive CNNC torsion. This is possible due to favorable energy gradients in S\textsubscript{1} while in S\textsubscript{0} the isomerization pathway is blocked by a large 1.5 eV barrier. At 105 fs after excitation, the nuclear wavepacket reaches the S\textsubscript{1}/S\textsubscript{0} CoIn. This is the decisive event common to many other photochemical reactions. Initially located only in S\textsubscript{1}, around the CoIn, parts of the wavepacket relax into S\textsubscript{0} and then continue to evolve toward the trans geometry at ±180°, where the photochemical reaction is completed. A vibronic coherence, characterized by an overlap of nuclear wavepackets in the two electronic states, emerges around the CoIn. The initial absence and subsequent emergence of this coherence is a unique signature of CoIns and is our target for spectroscopic detection.

The ultrafast XRD imaging of molecular dynamics is sketched in Figure 2A. First, an optical pump excites the molecule from S\textsubscript{0} to S\textsubscript{1} thus initiating the photochemistry. After a variable time-delay T\textsubscript{i}, an X-ray pulse with wave vector \( k_x \) that is off-resonant with respect to all molecular transitions is scattered off the electron density. The scattered photons \( k_x \) are recorded on the detector versus the momentum transfer \( \mathbf{q} = k_x - k_i \), yielding a diffraction pattern. In the absence of long-range crystalline order, the usually dominating Bragg peaks vanish and the pattern is more smooth.

The loop diagrams in Figure 2B represent all terms that contribute to the diffraction signal in a two-electronic-states model system. They can be partitioned into three classes. The first is elastic and inelastic scattering from the ground state, and the second from the excited state. Both classes are based on the populations \( \rho_i(\mathbf{q}|\mathbf{x}) \) with \( i = \{ e, g \} \) of the normalized nuclear populations. A pump pulse \( \epsilon_p \) excites azobenzene and initiates the photoisomerization in S\textsubscript{1}. A time-delayed X-ray probe pulse with envelope \( \epsilon_R \) images the molecular structure by elastic and inelastic photon scattering. An additional resonant infrared field significantly enhances the coherence while leaving the product yield unaffected. (B) Loop diagrams of the single-molecule diffraction signal. The pump pulse brings the molecule into the excited state by two interactions, one with the bra and one with the ket. The molecule then undergoes nonadiabatic dynamics marked by the shaded grey area, bringing it into a superposition which includes the coherence density matrix elements eg and ge. The coherence at the conical intersection is amplified by the IR field and probed via combined elastic/inelastic X-ray scattering. Detailed diagram rules are given in the SI. Labeling of the individual loops (i)–(v) corresponds to eq 1.
wavepackets $|\chi_i\rangle$ in the respective state $i$. The third class involves the coherences $\rho_{eg}|\chi_e\rangle\langle\chi_g|$, characterized by a nuclear wavepacket overlap that is intrinsically much weaker. Additionally, the population terms include scattering from electronic state densities $\delta_i(q)$, where all 96 electrons of the azobenzene molecule contribute. In contrast, the purely electronic coherence terms also contain inelastic scattering from transition densities $\sigma_{ij}$ where only one (or a few) active electrons that corresponds to the excitation character (here, an electron from a nitrogen n-orbital) contribute.

The diffraction signal represented by diagrams i–v in Figure 2B is given by

$$S(q, T) \propto N \int dt E_\gamma(t - T)^2$$

$$\rho_{eg}(t)|\chi_e(t)\rangle\langle\chi_g(t)|$$  \hspace{1cm} (i)  

$$+ \rho_{ee}(t)|\chi_e(t)\rangle\langle\chi_e(t)|$$  \hspace{1cm} (ii)  

$$+ \rho_{ee}(t)|\chi_e(t)\rangle\langle\chi_e(t)|$$  \hspace{1cm} (iii)  

$$+ \rho_{ee}(t)|\chi_e(t)\rangle\langle\chi_e(t)|$$  \hspace{1cm} (iv)  

$$+ 2\rho_e(t)|\chi_e(t)\rangle\langle\chi_g(t)|$$  \hspace{1cm} (v)  

$$+ \rho_e(t)|\chi_g(t)\rangle\langle\chi_g(t)|$$  \hspace{1cm} (vi)  

(1)

It depends on the X-ray probe pulse envelope $E_\gamma(t - T)$, taken to be a Gaussian with 2 fs full width at half-maximum (FWHM), the time delay $T$, the number of molecules $N$, and we write $\delta = \delta(q, R)$ for brevity. As indicated in Figure 2A, we propose employing an additional IR field at the same time delay as $E_\gamma$. The IR pulse amplifies the signals differentially by introducing a resonance (pole in the complex plane) at the small energy gap in the vicinity of the CoIn. Small amounts of population in this region are shifted around between the two electronic states, enhancing the wavepacket overlap and thus the coherence. In our simulations, the IR field is included in the propagation of $\chi(t)$ and thus does not appear explicitly in the signal expression (eq 1). In eq 2 and the SI we derive perturbative expressions in the IR field by including it at the signal stage but not in the propagation, leading to an amplification term when it is resonant with the energy gap around the CoIn.

The $\sigma_{ij}$ in eq 1 remain operators in the nuclear space after taking their matrix elements in the adiabatic electronic subspace. Once recorded in momentum space, stationary diffraction patterns can be translated to real space to obtain the electron density $\hat{\sigma}(r)$ and thereby the molecular structure. There are a few problems with this inversion, i.e., the phase problem related to the fact that only absolute amplitudes are recorded and the phases are therefore lost. An extensive literature exists that solves this problem, e.g., by oversampling or by anomalous diffraction. Phase retrieval for structure reconstruction is still scarce in femtosecond X-ray diffraction studies as this is a difficult task with many technical subtleties and pitfalls. Nonetheless, phase retrieval is being achieved in increasingly more challenging situations. It is not clear which method is most suitable for phase retrieval in our proposed experiment. Here, we focus on predicting and explaining what can be learned about CoIns from the diffraction patterns. Recently, we have shown that oscillations in the coherence term $(v)$ in eq 1 correspond to phase changes of the electron transition density in real-space.

While eq 1 yields the total diffraction pattern that monitors the photochemical reaction, it is desirable to isolate contributions of individual diagrams. Structure determination in the ground state is straightforward, and separate imaging of excited-state structures could be enabled by targeting terms ii and iv. The most intriguing possibility is the direct imaging of the charge density at CoIns by isolating term v.

We employ OCT to investigate both excited-state and coherence amplification possibilities. In this approach, laser pulses are usually shaped to prepare a targeted quantum state at a desired time. Numerous other control aims have been achieved experimentally in chemistry and biology demonstrating the potential of laser-steered molecular dynamics. Technically, the algorithm works via iterative maximization of a global control functional by shaping the temporal structure of the controlling laser field. OCT holds

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**Figure 3.** (A) Population dynamics (top), coherence magnitudes (black), laser pulses (orange), and spectrograms (bottom) using only a visible field. (B) With additional IR field at 105 fs delay. (C) With IR field at 130 fs delay. The additional IR field in B and C enhances the coherence magnitude while leaving the population dynamics and thus the photochemical reaction intact. The shaded red area in B and C indicates the time where the IR field is active.
promise to directly amplify spectroscopic features as well,\textsuperscript{48,49} as will be demonstrated here. By examining the loop diagrams in Figure 2B, we identify three groups of diagrams that can potentially be maximized at desired times. The first is diagrams i and iii related to the ground-state population $|g⟩⟨g|$ and is trivially achieved by removing the optical pump $ε_p$, leaving azobenzene in the electronic ground state. The second group consists of diagrams ii and iv, associated with the excited-state population $|e⟩⟨e|$. This means shaping $ε_p$ to achieve maximum population transfer from $S_0$ to $S_1$, potentially enabling direct excited-state structure determination. The third group (diagrams v) is the most interesting for us and involves the coherences $|g⟩⟨e|$. Being buried in the total diffraction signal by elastic scattering from $|g⟩⟨g|$ and $|e⟩⟨e|$ maximization of this contribution should enable the direct imaging of CoIn charge densities.

\section*{THEORETICAL SELECTION OF QUANTUM PATHWAYS}

We first explore the optimization of individual quantum pathways that contribute to the XRD signal. OCT\textsuperscript{70} is employed to tailor laser pulses that prepare specific states associated with these pathways at desired times. Our first optimization aim is to prepare the $|e⟩⟨e|$ state, such that pathways ii and iv and thereby scattering from the electronically excited state dominates the total XRD signal. This is accomplished by employing an optical laser field with a wavelength tuned to the $S_0$ to $S_1$ transition, which is around 430 nm for the cis geometry of azobenzene. Starting with a Gaussian laser field envelope, the optimized laser pulse that maximizes $|e⟩⟨e|$ at 25 fs, i.e., shortly after the pulse in time, is shown in Figure 3A.

It has an almost perfect Gaussian shape with a fwhm of 10 fs and achieves 80% population transfer from $S_0$ to $S_1$. Higher yields are possible but come at the cost of increased pulse intensity and complexity, which might initiate undesired multiphoton processes. In a recent diffraction experiment on the retinal photosensitization in bacteriorhodopsin,\textsuperscript{20} a power titration of the optical pump had found that deviation from the linear regime occurs at about 30 GW cm$^{-2}$. Our pump pulse in Figure 3A exhibits an electric field strength of around 6 GV/cm, which amounts to an intensity of below 5 GW cm$^{-2}$. Multiphoton processes are thus unlikely, and 80% excitation is sufficient to achieve a dominating $|e⟩⟨e|$ contribution in the diffraction signal. This is demonstrated in Figure 4, which depicts the total diffraction signal using the pulse of Figure 3A, together with the relative magnitude of the elastic excited-state scattering term ii in eq 1.

Initially vanishing prior to the pump, this relative magnitude gets very large and dominates the diffraction signal after the action of $ε_p$. The total diffraction signal does not change yet, since the ground- and excited-state electron densities are very similar, and the nuclear wavepacket is located at the same geometry. Nevertheless, between 0 and 150 fs, it is mainly dominated by the term ii in eq 1, allowing for the transient monitoring of excited-state structures on the photochemical pathway.

Note that practically, in typical "laser on minus laser off" experiments, the ground-state contribution could simply be subtracted to obtain the excited-state signal without any shaping. As demonstrated in recent similar experiments,\textsuperscript{54,51} the detection limit for weak features still critically relies on the fraction of excited molecules. Using OCT to significantly enhance this can be beneficial. Additionally, in azobenzene cis $\rightarrow$ trans photoisomerization, only one excited state $S_1$ contributes to the photochemistry, and subtracting the ground state yields the contribution of this state. Other molecules and processes might involve two or more excited states, where this specificity no longer holds. Using the same OCT presented here, the population in individual states can be maximized, thus allowing for detection of their specific signatures. Referring to Figure 2B, introducing more excited states $ε$ adds a new group of loop diagrams that each contribute to the total diffraction signal. Using the same OCT, each quantum pathway can be individually addressed, allowing to acquire more detailed information about the photochemical mechanism.

Besides the optimal laser pulse and its spectrogram, Figure 3A also depicts the cis $\rightarrow$ trans photoisomerization kinetics. After initial excitation, the CoIn seam is reached at around 100 fs, and the nuclear wavepacket relaxes back to the ground state. Once reaching the product minimum of trans azobenzene at $\pm 180^\circ$, it is absorbed and not considered further. The population in the trans minimum is marked by the magenta line in Figure 3A and slowly reaches over 40% within 900 fs.

Our second goal is to maximize the coherence $ρ_{ eg}$ magnitude at the CoIn passage. This should enhance pathways v in Figure 2 and eq 1. After being very strong during the optical excitation, as the wavepacket is equally distributed between $S_0$ and $S_1$ during the population transfer, $ρ_{ eg}$ is almost vanishing during the CoIn passage. As demonstrated in previous studies,\textsuperscript{12} the coherence term is strongest at high momentum transfer amplitudes $q$. This is because the electron transition densities $σ_q( r)$ are more confined in real space than the state densities $σ_q( r)$, as only a single electron from a nitrogen orbital contributes. The quantity determining the strength of the coherence term $v$ at high $q$ is $|g⟩⟨e|$, which we directly optimize with OCT. We use the projection operator depicted in Figure S2 to maximize $|g⟩⟨e|$ at 105 fs, where the major CoIn passage takes place. This projection operator restricts the evaluation of...
the control functional to a specific region in the nuclear space thus ensuring selectivity to the CoIn.

We first tried to optimize the optical pump $\varepsilon_p$ by employing temporal and frequency constraints, which did not yield significant results. Instead, after removing the constraints, the algorithm converges to an additional field directly centered around 105 fs with an almost Gaussian envelope and a frequency range in the IR regime. The approach clearly works, as demonstrated in Figure 3B. The almost vanishing coherence $\rho_{q\varepsilon}$ at 105 fs without the IR field is now greatly enhanced. Importantly, as can be seen from the population dynamics in Figure 3B, and especially the product yield, the photochemical reaction remains intact. This ensures that the photochemical process is observed in its natural form, without modifying it during the observation. The IR field in Figure 3B is surprisingly smooth, in contrast to the more complicated temporal profiles usually obtained after many OCT cycles. The proposed scheme is thus readily feasible and does not require an elaborate pulse shaping.

The effect of IR amplification on the diffraction signal is shown in Figure 5. The signal (eq 1) is given by the radial average over molecular orientations and drawn vs time delay and the scattering vector $q$. Using only the visible pump laser pulse and no IR field, the coherence term in the diffraction signal is very weak in Figure 5A. Employing the IR field at 105 and 130 fs significantly amplifies this contribution, achieving the control aim. This is further exemplified in Figure 5D–F, which shows the relative magnitude of the coherence term in the total diffraction signal. Being well below $10^{-3}$ in the absence of the IR field, and thus much weaker than other contributions and probably not detectable, this significantly changes when the IR field is employed. The coherence term is amplified by at least 1 order of magnitude, reaching 1% relative strength at high $q$ and precisely at the time of the CoIn passage. In combination with other techniques for further separating the coherence term, e.g., frequency-resolved diffraction,\(^{52}\) the IR field could bring this signature above the detection threshold. In recent scattering experiments, a detection limit of 0.05% for a perfectly excited sample has been reported,\(^{53}\) and oscillatory features with 4% relative strength have been resolved for a weakly excited sample.\(^{9}\) These numbers are comparable to the coherence term strength in Figure 5B assuming 80% excitation, which should thus be detectable.

**EXPERIMENTAL REALIZATIONS**

In experiment, only the total diffraction signal—and not the individual quantum pathways—is observed. Additionally, optimal control experiments (OCE) work fundamentally differently from OCT. While in OCT individual quantum pathways, represented by the loop diagrams in Figure 2B, can be optimized, in OCE the control problem is solved by feeding the spectral output after sample interaction to an evolutionary algorithm, and optimizing for a desired contribution. Laser pulses are dispersed onto a liquid crystal spatial light modulator, where individual pixels can be modified to suppress specific pulse frequencies.\(^{42,53}\) This major discrepancy had always complicated the practical implementation of OCT.

Here, we present a novel strategy that is directly achievable in OCE. No a priori knowledge about the CoIn is necessary. An IR field with frequencies of a few tenths of eV or below will only induce a resonant coherence amplification when the electronic states get very close in energy, i.e., exactly at CoIns. A generic IR field resembling the one in Figure 3B can be used in coincidence with the X-ray probe field at variable time delays. Only when the molecule goes through a CoIn passage will the XRD diffraction at high momentum transfer $q$ exhibit oscillatory features resembling the ones in Figure 5. This is exemplified in Figures 3C and 5C where the pulse optimized for 105 fs is also effective at 130 fs and exhibiting a very smooth Gaussian shape. The oscillatory spectral output from Figure 5 can then be relayed to the genetic algorithm used experimentally to optimize the IR field exactly for this feature and enhance it even more.

Once the optimal solution to this control problem is found, information about the CoIn itself can be retrieved from the pulse spectrogram. In our case, the IR field in Figure 3 is centered around 5 μm, i.e., 0.25 eV. This exactly matches the energy difference between
SUMMARY

We demonstrated the ability of infrared fields to help the direct imaging of conical intersections. The corresponding signature in the time-resolved X-ray diffraction signal is significantly amplified by resonantly enhancing the coherence magnitude. This signature may not be observable otherwise since the total signal is dominated by the much stronger elastic scattering contributions that give no information about conical intersections. Employing an IR field that maximizes the coherence can be the crucial factor in making direct imaging of conical intersections possible, potentially revolutionizing the understanding of ultrafast photochemistry. The results are demonstrated for azobenzene photoisomerization, which is widely applied in chemistry, biology and pharmacology, and provides a typical textbook conical intersection passage as found in many other molecules and systems. The laser pulses are optimized with optimal control theory, ensuring their maximal success, and are surprisingly smooth and simple. The energetic topology of the conical intersection can be read from the optimized laser field spectrogram. The present approach is readily translatable to other molecules, provided that there exists a non-vanishing transition dipole in the conical intersection vicinity. The IR field leaves the photochemistry intact and, thus, provides a noninvasive amplification of molecular coherences in the naturally occurring mechanism.

METHODS

To perform exact nuclear wavepacket simulations of azobenzene photoisomerization, we select two reactive nuclear degrees of freedom. The torsion angle between the nitrogen and the two connected carbon atoms connects the cis geometry at CNNC = 0° to the trans at CNNC = 180° and is thus the active isomerization coordinate. The bending angle between the two nitrogen atoms and one adjacent carbon atom is the second coordinate while the other CNN angle remains fixed. This symmetry breaking is necessary in order to reach the minimum energy conical intersection seam.

The effective Hamiltonian describing the coupled nuclear and electronic degrees of freedom, in the space of the two nuclear coordinates R1 and R2, is given by

\[
\hat{H} = \hat{T} + \hat{V}(\text{R}) - \epsilon(1)\hat{\theta}_{\text{R}}(\text{R}) + \hat{K}_{\text{R}} - \epsilon(1)\hat{\varphi}_{\text{R}}(\text{R}) - \hat{K}_{\varphi} \hat{\varphi}(\text{R})
\]

The potential energy surfaces \(\hat{V}(\text{R})\) for the ground state g and excited state \(\epsilon(1)\) were computed using high-level CASPT2 with an active space of 18 electrons in 16 orbitals (all six \(\pi^*\) orbitals and two nitrogen \(n\)-orbitals) with the MOLCAS8 program package \(62,63\) and the ANO-L-VDZP basis set \(64\). They were discretized on a numerical grid with 600 points in CNCN and 256 in CNN.

The kinetic energy operator \(\hat{T}\) in eq 3 in the G-Matrix formalism is given by

\[
\hat{T} \approx -\frac{\hbar^2}{2m} \sum_{i=1}^{2} \sum_{j=1}^{2} \rho_{ij} \frac{\partial^2}{\partial q_i \partial q_j}
\]

with \(\rho_{ij} \in \mathbb{R}\) and the G-Matrix computed via its inverse elements

\[
(G^{-1})_{pq} = \sum_{i=1}^{\infty} \frac{\partial \chi_i}{\partial q_p} \frac{\partial \chi_i}{\partial q_q}
\]

\(\hat{K}_{\text{R}}\) in eq 3 approximates the non-adiabatic couplings and is given by

\[
\hat{K}_{\text{R}} \approx \frac{1}{2m} \sum_{i=1}^{12} \frac{\partial \chi_i}{\partial \text{R}} \frac{\partial \chi_i}{\partial \text{R}}
\]

and \(f_{\text{R}}\) contains terms \(\Phi(m)\) with the electronic wave function \(\Phi\).

The nuclear wave function \(\chi(\text{R}, t)\) is obtained by propagating the \(S_0\) ground state vibrational wave function \(\psi(\text{R}, t_0)\) with a Chebychev propagator using a time step of 0.05 fs. Periodic boundary conditions are employed along CNCN in \(S_2\) while in \(S_0\) a Butterworth filter \(65\) absorbs the wavepacket at CNNC = ±180°. All terms \(i\approx\psi\) in the diffraction signal (eq 1) were evaluated every 0.5 fs. This requires the state and transition densities \(\sigma_i(q, R)\), which remain

\(S_1\) and \(S_0\) at the CNN in Figure 1B. In this respect, the IR field does not only act as an amplification of the X-ray probe but also as a direct probe of energetic topologies around CoIns. This approach is universally applicable to a wide range of photochemical reactions to amplify coherences and thereby decipher CoIn dynamics.

Our proposed IR control scheme works particularly well for short time scales in efficient photochemical reactions like azobenzene isomerization, where the nuclear motion is coherently funneled into specific pathways. At longer times, internal vibrational relaxation to other nuclear degrees of freedom takes place, and the molecule explores a much larger conformational space. Any near-degeneracy region between two electronic states with a nonvanishing transition dipole will then contribute to the IR-induced signal. The latter is then no longer specific to CoIns, since besides near-degeneracy, it does not depend on unique CoIn signatures like, e.g., the geometric phase, \(45\) for which sensitive experimental signatures have not been identified yet.

The resonant amplification via an IR field can be rationalized by including it in eq 1. In the Supporting Information, we derive expressions for the ultrafast XRD signal perturbed at second order by the IR field with envelope \(E_{\text{IR}}\) and central frequency \(\omega_{\text{IR}}\).

The coherence term then reads

\[
S_{\text{XRD}}(q, T, \omega_{\text{IR}}) \propto \text{Re} \left[ \rho_{ge} \frac{\partial}{\partial \epsilon} \left( \omega_{\text{IR}} - \omega_{\text{IR}} + \omega \right) \left| \langle \epsilon | \hat{\theta}_q | g \rangle \right|^2 \right] \int dt \left\{ \rho_{ge}(1 - T) \right\} \times \left\{ \langle \epsilon | \hat{\theta}_q | g \rangle \right\}
\]

where \(\rho_{ge}\) are transition dipole matrix elements between the g and \(\epsilon\) state, in this case taken to be an average over the nuclear space near the CoIn. In comparison to eq 1, we obtain a resonance factor when the IR field central frequency matches the average energy difference between the PES at delay \(T\). Again, this loses specificity at longer time scales, since any near-degeneracy region in the high-dimensional nuclear space will induce a resonance factor. The advantage of the OCT scheme is that it can readily find the IR pulse central frequency that enhances the coherence contribution in the signal at a desired delay without a priori knowledge of the CoIn geometry. Alternatively, the OCT can be used to map the energy difference experienced by the wavepacket at that delay.

A competing technique to XRD at FELs is ultrafast electron diffraction (UED) at dedicated facilities. \(60-66\) Instead of photon pulses, ultrabright electron pulses are used to record diffraction patterns from molecules. In addition to scattering off electron densities, the electron pulses also scatter off the nuclear charge density. With respect to eq 1, all terms are contained in the UED signal as well, while interesting terms involving the nuclear charge density and mixed nuclear + electronic terms come into play. It has been experimentally demonstrated that structural and electronic dynamics can be simultaneously recorded in a single UED experiment. \(60\) In particular, the retrieval of local molecular information at high momentum transfer amplitudes, as reported here for CoIns, has been demonstrated there as well by detecting the local n-hole of the nitrogen atom in pyridine. Given the similarity of the XRD and UED signal in the rigorous quantum-electrodynamical framework, \(67\) employed in eq 1, our proposed IR enhancement of molecular coherences is expected to apply to UED as well. Recent simulations of the UED signal for \(\text{trans} \rightarrow \text{cis}\) isomerization of azobenzene have already demonstrated the sensitivity of this signal to ultrafast molecular motions. \(45\)
operators in the nuclear space and were evaluated in $2^\circ$ increments from the state specific charge density matrices $P_i$ according to

$$\sigma_{\alpha}(\mathbf{r}, \mathbf{R}) = \int d\mathbf{r} e^{i\mathbf{q}\cdot \mathbf{r}} \sum_{\mathbf{R}_n} f_{\alpha}(\mathbf{R}_n) \phi_{\alpha}(\mathbf{r}, \mathbf{R})$$

using the basis set of atomic orbitals $\phi_{\alpha}(\mathbf{r})$.

Laser pulses were optimized by OCT through iterative maximization of the functional $F_i$:

$$F_i = \int dt - \int_0^T \psi_i(\mathbf{t}) G_i(\mathbf{t}), \epsilon(\mathbf{t}) \psi_i(\mathbf{t}) dt$$

with the initial and final wave functions $\psi_i(\mathbf{t})$ and $\psi_f(\mathbf{t})$, and with $G_i(\psi_i(\mathbf{t}), \epsilon(\mathbf{t}))$ representing the time-dependent Schrödinger equation. $F_i(\psi_i(\mathbf{t}))$ denotes the optimization aim

$$F_i(\psi_i(\mathbf{t})) = (\psi_i(\mathbf{T})|\psi_i(\mathbf{T}))$$

where we use the projection operator $\mathbf{P} = \psi_i(\mathbf{T})\psi_i(\mathbf{T})$. The function $\epsilon(\mathbf{t})$ in eq $8$ contains the Krotov change parameter $\alpha$ that penalizes high pulse intensities, a shape function to ensure smooth switching on and off behavior of the laser field, and a filter operation in the frequency domain to keep the pulse within a defined spectral range.

Pulse spectrograms depicted in Figure 3 were calculated by

$$I_{\text{PROC}}(\omega, T) = \int_{-\infty}^{\infty} \psi_i(\mathbf{t}) E_{\text{gap}}(\mathbf{t} - T) e^{-\alpha \omega^2} dt$$

corresponding to a frequency–resolved optical gating measurement.¹¹

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Loop Diagram Rules

Loop diagrams that contribute to the time–resolved diffraction signal are shown in Fig. 2 in the main manuscript. The Diagram rules are as follows:\textsuperscript{S1}

- Time runs along the loop clockwise from bottom left to bottom right.
- Each field interaction is represented by an arrow, which either points to the right (photon annihilation and excitation of the molecule) or to the left (photon creation and de–excitation of the molecule).
• Free evolution periods on the left branch indicate forward propagation in real time, and on the right branch to backward propagation respectively.

• The last field interaction (in this case, $k_x$) is the detected photon mode. In addition, the gray bar represents the period of free evolution.

Signal derivation

The ultrafast XRD signal can be written as

$$S_{\text{XRD}}(q, T) \propto |\epsilon_x \cdot \epsilon_s|^2 \text{Re} \int dt |E_x(t-T)|^2 \langle \Psi(t) | \sigma^\dagger (-q) \sigma(q) | \Psi(t) \rangle$$

where $q = k_s - k_x$ is the momentum transfer, $T$ the delay between the actinic pulse and the diffracted X-ray pulse, $|\epsilon_x \cdot \epsilon_s|^2$ is the Lorentz polarization factor (omitted in the following), $A_x(t)$ is the X-ray pulse time envelope, $\sigma$ is the molecular charge density, and $|\Psi(t)\rangle$ is the many-body molecular wavefunction.

In the main text, we have shown how an OCT scheme that maximizes the coherence contribution in the ultrafast XRD signal leads to the addition of an IR field coincident with the X-ray pulse. Here, we derive the signal expression of the ultrafast XRD signal using second order perturbation theory in the resulting IR field and show how the coherence contribution is indeed maximized due to a resonance effect. This calculation demonstrates that the resonance induced by the IR field is responsible for the amplification. This derivation should not obscure the advantage of the OCT that naturally finds the optimal IR field without a priori knowledge of the CoIn geometry.

To first order in the IR field, no mixed terms $\sigma_e \sigma_g$ involving a coherence shows up.
We thus expand the signal to second order in the IR field:

\[
S_{\text{XRD}}(q, T, \omega_{\text{IR}}) \propto \text{Re}(\text{−}1)(-\frac{i}{\hbar})^2 \int dt dt_1 dt_2 |A_x(t - T)|^2 E^*_{\text{IR}}(t - t_1 - T)E_{\text{IR}}(t - t_2 - T) \times \langle \Psi(t - t_1)|\mu G^\dagger(t_1)\sigma^\dagger(-q)\sigma(q)G^\dagger(t_2)\mu^\dagger|\Psi(t - t_2) \rangle \tag{2}
\]

where \(\mu\) is the electric dipole operator, \(E_{\text{IR}}(t)\) is the IR field and \(\omega_{\text{IR}}\) is the IR field central frequency contained implicitly in \(E_{\text{IR}}(t)\). The XRD signal is usually derived in the velocity gauge and one must carefully treat the conversion of the electric transition dipole into this gauge from the length gauge. Here, the terms arising from this transformation are absorbed in the definition of the proportionality coefficient.

Writing the IR field in the frequency domain \(E_{\text{IR}}(t - t_1 - T) = \int d\omega /(2\pi) E_{\text{IR}}(\omega)e^{-i\omega(t-t_1-T)}\) allows to rewrite the signal as:

\[
S_{\text{XRD}}(q, T, \omega_{\text{IR}}) \propto \text{Re} \int dt dt_1 dt_2 d\omega_1 d\omega_2 |A_x(t - T)|^2 E^*_{\text{IR}}(\omega_1)E_{\text{IR}}(\omega_2) \times \langle \Psi(t - t_1)|\mu G^\dagger(t_1)\sigma^\dagger(-q)\sigma(q)G(t_2)\mu^\dagger|\Psi(t - t_2) \rangle e^{i\omega_1(t-t_1-T)}e^{-i\omega_2(t-t_2-T)} \tag{3}
\]

We now sum over electronic states and express the signal correlation function in terms of a normalized nuclear wavepacket \(|\chi_i(t)\rangle\):

\[
S_{\text{XRD}}(q, T, \omega_{\text{IR}}) \propto \text{Re} \sum_{ij\ell m} \int dt dt_1 dt_2 d\omega_1 d\omega_2 \rho_{ij}(t)|A_x(t - T)|^2 E^*_{\text{IR}}(\omega_1)E_{\text{IR}}(\omega_2) \times \langle \chi_j(t - t_1)|\mu_{ij} G^\dagger(t_1)\sigma^\dagger(-q)\sigma(q)G_{\ell m}(t_2)\mu^\dagger_{\ell m}|\chi_i(t - t_2) \rangle e^{i\omega_1(t-t_1-T)}e^{-i\omega_2(t-t_2-T)} \tag{4}
\]

where \(\mu_{ij}, G_l(t_1)\) and \(\sigma_{ij}(q)\) are still operators in nuclear space. The two terms in Eq. 4 correspond to the two loop diagrams displayed in Fig. S1.

Multiple approximations are needed to simplify the expression for the signal in order to highlight the resonant amplification. First, we assume that the nuclear wavepacket is sufficiently localized in each PES, so that the electronic energy is approximately constant
Figure S1: Loop diagrams representing contributions to the ultrafast XRD signal in the presence of an extra IR field (red arrows). a) General term in the summation of Eq. 4. b) Loop diagram for the coherence-sensitive contribution to the signal, Eq. 8.

in its region. We can then set $G_f(t_1) \simeq \theta(t_1)e^{-(i/h)E_l t_1}$. Similarly, we assume that the transition electric dipoles do not vary appreciably in the small region in the vicinity of the CoIn and are thus scalars in nuclear space. Finally, we assume that the integration time $t_1$ is short so that no appreciable nuclear dynamics happens during that time and thus $|\chi_i(t - t_1)\rangle = G_f^\dagger(t_1)|\chi_i(t)\rangle$. These approximations yield for the signal:

$$S_{\text{XRD}}(q, T, \omega_{\text{IR}}) \propto \Re \sum_{ijklm} \int dt_1 dt_2 d\omega_1 d\omega_2 \rho_{ji}(t)|A_x(t - T)|^2 E_{\text{IR}}^*(\omega_1)E_{\text{IR}}(\omega_2)$$

$$\times \langle \chi_j(t) | \sigma_{ml}^+(q) \sigma_{mk}(q) | \chi_i(t) \rangle \mu_{lj}^* \mu_{ki} e^{i(\omega_{lj} - \omega_1)t_1} e^{i(\omega_{ki} - \omega_2)t_2} e^{i\omega_1(t - T)} e^{-i\omega_2(t - T)}$$

(5)

The integrals over $t_1$ and $t_2$ can then be calculated:

$$S_{\text{XRD}}(q, T, \omega_{\text{IR}}) \propto \Re \sum_{ijklm} \int dt_1 dt_2 d\omega_1 d\omega_2 \rho_{ji}(t)|A_x(t - T)|^2 E_{\text{IR}}^*(\omega_1)E_{\text{IR}}(\omega_2)$$

$$\times \langle \chi_j(t) | \sigma_{ml}^+(q) \sigma_{mk}(q) | \chi_i(t) \rangle \mu_{lj}^* \mu_{ki} \frac{i}{\omega_{lj} - \omega_1 + i\epsilon} \frac{-i}{\omega_{ki} - \omega_2 + i\epsilon} e^{i\omega_1(t - T)} e^{-i\omega_2(t - T)}$$

(6)

Finally, by assuming that the IR field is long compared to the X-ray field (OCT pro-
vides an IR field of about 50 fs and the X-ray field is typically few fs long or shorter), we can further simplify the expression into:

\[
S_{XRD}(q, T, \omega_{IR}) \propto \text{Re} \sum_{ijklm} \int dt \rho_{ji}(t) |A_x(t - T)|^2 |E_{IR}(\omega_{IR})|^2 \\
\times \langle \chi_j(t) | \sigma_{ml}^\dagger(-q) \sigma_{mk}(q) | \chi_i(t) \rangle \frac{\mu_{ij} \mu_{ki}}{(\omega_{ij} - \omega_{IR} + i\epsilon)(\omega_{ki} - \omega_{IR} + i\epsilon)} \tag{7}
\]

Here, we see that coherence terms can have a resonance factor when the IR field central frequency matches the average energy difference between the PES at the delay \( T \). The resulting expression for the coherence is given by:

\[
S_{XRD}(q, T, \omega_{IR}) \propto \text{Re} \frac{\mu_{ge} \mu_{eg} |E_{IR}(\omega_{IR})|^2}{(\omega_{ge} - \omega_{IR} + i\epsilon)(\omega_{eg} - \omega_{IR} + i\epsilon)} \int dt \rho_{ji}(t) |A_x(t - T)|^2 \\
\times \langle \chi_e(t) | \sigma_{eg}^\dagger(-q) \sigma_{ee}(q) | \chi_g(t) \rangle \tag{8}
\]
Projection operator

Figure S2: Projection operator used in OCT optimizations to maximize coherence amplification at the conical intersection. The $S_0$ (bottom) and $S_1$ (top) surfaces are drawn for reference. The projection operator has a value of 0 in the shaded area and 1 in the highlighted area, where the conical intersection is located.

References
