# SUPEREXCHANGE AND ELECTRON TRANSFER IN THE PHOTOSYNTHETIC REACTION CENTER

Yuming HU and Shaul MUKAMEL<sup>1</sup>

Chemistry Department, University of Rochester, Rochester, NY 14627, USA

Received 22 May 1989

The relative magnitude of the sequential and superexchange electron transfer mechanisms in the primary electron transfer event in a reaction center is a controversial issue. One complication in resolving this problem is that the conventional superexchange theory is valid only when the intermediate energy level is sufficiently high. The precise position of this level in the reaction center is not known, and it is not clear whether this condition is met. We present a novel expression for the superexchange rate in a threelevel system, which holds for arbitrary values of the system free energies and reorganization energies. Implications as to the relative contribution of the superexchange and sequential mechanisms are discussed.

## 1. Introduction

The mechanism for fast electron transfer in reaction centers is one of the many interesting puzzles in understanding the primary events in photosynthesis [1,2]. In the photosynthetic reaction center an electron moves in 2.8 ps over a distance of 17 Å from a bacteriochlorophyll dimer (P) to bacteriopheophytin (H) via an intermediate bacteriochlorophyll monomer (B). The model system suggested for the electron transfer in the reaction center (RC) [3,4] involves three electronic configurations. Using the notation of Marcus, we denote these states (P\*BH,  $P^+B^-H$  and  $P^+BH^-$ ) as  $|1\rangle$ ,  $|2\rangle$ , and  $|3\rangle$ , respectively. State  $|1\rangle$  is the optically excited chlorophyll dimer state, state  $|3\rangle$  is the charge transfer state observed after 2.8 ps and state  $|2\rangle$  is a possible intermediate state. The complete kinetic scheme for this system involves a  $3 \times 3$  rate matrix whose matrix elements  $K_{in}$  denotes the transition rate from state  $|n\rangle$  to state  $|j\rangle$ ; n, j=1, 2, 3. Since a direct (through space) coupling between states  $|1\rangle$  and  $|3\rangle$  is excluded by the large separation of P and H, there are two basic mechanisms that have been suggested for the electron transfer process [3,4]. The first is superexchange, whereby  $|2\rangle$  serves as an intermediate virtual state. When level  $|2\rangle$  is sufficiently higher in energy than  $|1\rangle$  and  $|3\rangle$  the superexchange rate is given by

$$K_{31} = \frac{2\pi}{\hbar} |V_{\rm SE}|^2 S.$$
 (1)

Here S is a Franck-Condon-weighted density of states and  $V_{\rm SE}$  is the superexchange coupling,

$$V_{\rm SE} = \frac{V_{12}V_{23}}{\Delta G_{12}^0 - \lambda_{12}}.$$
 (2)

 $\Delta G_{12}^0$  is the free energy difference between states  $|1\rangle$ and  $|2\rangle$ ,  $\lambda_{12}$  is the corresponding reorganization energy [5] and  $V_{in}$  is the electronic coupling between states  $|j\rangle$  and  $|n\rangle$ . The other possible mechanism involves a sequential process whereby the electron transfers from level  $|1\rangle$  to  $|2\rangle$  and then from  $|2\rangle$ to  $|3\rangle$ . This mechanism is described by rates  $K_{21}$  and  $K_{32}$  and does not involve  $K_{31}$ . In the superexchange mechanism level  $|2\rangle$  is never populated and the electron tunnels from level  $|1\rangle$  to  $|3\rangle$ . Level  $|2\rangle$ simply contributes to the tunneling matrix element (eq. (2)). Another way of stating this is that due to the energy-time uncertainty relation, the system can spend only a very short time  $\approx \hbar/(\Delta G_{12}^0 - \lambda_{12})$  in that level. Consequently, the dynamics of level  $|2\rangle$ does not affect the rate. All we need to know is its thermally averaged energy. In the sequential mech-

<sup>&</sup>lt;sup>1</sup> Camille and Henry Dreyfus Teacher/Scholar.

anism on the other hand, level  $|2\rangle$  is intermediate in the kinetic scheme  $|1\rangle \rightarrow |2\rangle \rightarrow |3\rangle$  and it could be populated during the course of the reaction. Ultrafast optical measurements [6] have shown that the rate of appearance of level |3> following the preparation of level  $|1\rangle$  by photoexcitation is  $3.6 \times 10^{11}$  s<sup>-1</sup>. These measurements have failed to detect a transient population of level |2>. This observation could support the superexchange mechanism. However, a sequential scheme with  $K_{32}$ /  $K_{21} \ge 70$  is also consistent with this result [7]. Extensive additional linear and nonlinear spectroscopic information (such as hole-burning and photon echo) is available for this system [8,9]. A major obstacle in resolving this issue is the lack of precise information regarding many of the relevant energetic parameters [3,4,10]. In particular the vertical transition energy  $\Delta G_{12}^0 - \lambda_{12}$  is not known. It should be emphasized that eqs. (1) and (2) hold only when  $\Delta G_{12}^0 - \lambda_{12}$  is large enough.  $V_{\rm SE}$  diverges when  $\Delta G_{12}^0 - \lambda_{12}$  vanishes. In this paper we report a microscopic determination of  $K_{31}$  obtained by formulating the problem using the density matrix in Liouville space. This formulation was applied previously to nonadiabatic and adiabatic electron transfer in a two-level system and has been used to explore the role of the dynamics of solvation in electron transfer processes [11]. Our expression is valid for any value of  $\Delta G_{12}^0 - \lambda_{12}$  and can therefore be used to explore the interplay between superexchange and sequential electron transfer even when all three levels are degenerate.

#### 2. Superexchange in a polar medium

We start our analysis by introducing the adiabatic (Born-Oppenheimer) model Hamiltonian for the system

$$H = \sum_{j=1}^{3} |j\rangle H_{j} \langle j| + V_{12} (|1\rangle \langle 2| + |2\rangle \langle 1|) + V_{23} (|2\rangle \langle 3| + |3\rangle \langle 2|).$$
(3)

Here  $H_j(Q)$  denotes the adiabatic Hamiltonian of the polar medium.  $V_{jn}$  represents the electronic coupling between states  $|n\rangle$  and  $|j\rangle$ . The direct coupling  $V_{13}$  between states  $|1\rangle$  and  $|3\rangle$  was neglected in eq. (3) due to the large (17 Å) distance between the P and H molecules in the reaction center. The nuclear Hamiltonian  $H_j(Q)$  can be partitioned into the following three terms:

$$H_i(Q) = E_j + H_{\mathbf{B}} + U_j, \qquad (4)$$

where  $E_j$  represents the electronic energy of the unsolvated state  $|j\rangle$  and  $H_B$  represents the Hamiltonian of the bath, i.e. the nuclei of the RC which form a polar medium.  $U_j$  denotes the interaction between the electronic system and the medium, which may be expressed in terms of the polarization of the bath P(r), and the electrostatic field  $D_j(r)$  produced by the charge distribution of the system in the  $|j\rangle$  state, i.e.

$$U_j = -\int \mathrm{d}\boldsymbol{r} \, \boldsymbol{D}_j(\boldsymbol{r}) \cdot \boldsymbol{P}(\boldsymbol{r}) \,. \tag{5}$$

It should be emphasized that  $U_i$  depends on a macroscopic number of polarization degrees of freedom P(r), which undergo complicated motions resulting from thermal fluctuations. The statistical properties of  $U_i$  contain all the relevant information for our problem. We shall model  $U_i$  as Gaussian random variables. This is a common assumption in electron transfer theories [5]. It has been recently verified by an extensive numerical simulation of outer sphere electron transfer in water [12]. Eqs. (3)-(5) constitute our basic model Hamiltonian for the RC and they can be used to evaluate the electron transfer rates. We shall now introduce the following equilibrium density matrices for the bath

$$\rho_{j} = \exp(-H_{j}/k_{\rm B}T)/\mathrm{Tr}\exp(-H_{j}/k_{\rm B}T),$$
  

$$j = \mathrm{B}, 1, 2, 3, \qquad (6)$$

where Tr denotes a trace over the bath degrees of freedom.  $\rho_{\rm B}$  is the density matrix of the bath in the absence of the electron transfer system.  $\rho_1$ ,  $\rho_2$  and  $\rho_3$  are the density matrices of the bath when the electron transfer system is in states 1, 2 and 3, respectively.

For the sake of simplicity we assume that the energy fluctuation  $U_j$  of the  $|j\rangle$  state is totally uncorrelated with the energy fluctuation  $U_n$  on any other state  $|n\rangle$ , i.e.

$$\operatorname{Tr}(U_j U_n \rho_{\mathrm{B}}) = 0, \quad j \neq n .$$
(7)

This is a reasonable assumption for electron transfer

in the RC, because the different electronic states represent configurations in which the electron resides on different parts of the RC, which have a different local environment, and their energy fluctuations are expected to be uncorrelated. The present calculation of the rate is based on formulating the dynamics in terms of the density matrix in Liouville space [11]. The formalism allows a perturbative expansion of the rate matrix  $K_{in}$  in a power series in the nonadiabatic coupling V. This formalism was developed for electron transfer in a two-level system resulting in general expressions for  $K_{21}$  and  $K_{32}$ . In this Letter we focus on the calculation of  $K_{31}$ . The calculation is very similar to the calculation of two-photon processes (two-photon absorption or fluorescence and Raman spectroscopy) [11,13]. The lowest order in  $V_{in}$  which contributes to  $K_{31}$  is fourth order. When the calculation is done in Liouville space we find that there are three Liouville space pathways which contribute to  $K_{31}$  in fourth order, i.e.

$$K_{31} = 2 \operatorname{Re}(K_{31}^{1} + K_{31}^{11} + K_{31}^{11}) .$$
(8)

These pathways are represented diagrammatically in fig. 1. Path I represents the process in which the electron transfers from state  $|1\rangle$  to state  $|3\rangle$  without actually passing through state  $|2\rangle$ . This is therefore a tunneling process. Paths II and III represent the process in which the electron does go through state  $|2\rangle$ , but before it equilibriates with the bath at state  $|2\rangle$ , the electron transfers to state  $|3\rangle$ . Of course, there is another process contributing to the population of state  $|3\rangle$ , i.e. the electron moving to state  $|2\rangle$ , equilibriating with the bath, and then transferring to state  $|3\rangle$ . This process is the sequential transfer, which is described by the rates  $K_{21}$  and  $K_{32}$ . If the relaxation of the system (RC and environment) is rapid enough, the contribution to  $K_{31}$  from paths II and III in fig. 1 can be ignored, so the only quantity we need to consider is  $K_{31}^{l}$ . This term can be evaluated using the static approximation for solvent fluctuations and assuming Gaussian statistics for  $U_{\mu}$ The details of these calculations will be given elsewhere. Here we only present the final results for  $K_{31}$ in the high temperature limit.  $K_{31}$  is given in terms of several physical quantities (fig. 2). We first define the free energy change for the  $|j\rangle$  to  $|n\rangle$  transition

$$\Delta G_{jn}^{0} \equiv \operatorname{Tr}(H_{j}\rho_{j}) - \operatorname{Tr}(H_{n}\rho_{n})$$
(9a)



Fig. 1. The three Liouville-space pathways [10] contributing to the rate  $K_{31}$  to fourth order in the nonadiabatic coupling. Each pair of indexes *jn* implies that the system is in the state  $|j\rangle \langle n|$ , where j = n stands for a population and  $j \neq n$  for a coherence. Each bond represents a nonadiabatic coupling V. There are six pathways which can lead from 11 (upper left corner) to 33 (lower right) in fourth order (four bonds). These pathways come in complex conjugate pairs so that we need consider only the three pathways shown I, II and III. Pathway I which does not pass through a population in level 2 (eq. (22)) represents the tunneling (superexchange) mechanism and was evaluated explicitly in the present theory. Pathways II and III represent a sequential noncauilibrium process whereby the system goes through level 2 and proceeds to state 3 before thermal equilibrium. The contribution of these pathways may be made arbitrarily small if the medium relaxation times are sufficiently rapid. These pathways were neglected in the present theory.



Fig. 2. Configuration coordinate scheme showing the transition free energy  $\Delta G_{21}^0$ , the reorganization energy  $\lambda_{12}$  and the vertical transition energy  $\Delta E_{21}$ . Similar schemes apply for the other pairs of levels (13 and 23).

and the vertical transition energy for this transition when the system is in state  $|1\rangle$ 

$$\Delta E_{jn} \equiv \operatorname{Tr}\left[\left(H_j - H_n\right)\rho_1\right]. \tag{9b}$$

We further define the solvent reorganization energy in the  $|j\rangle$  state,

$$\lambda_i \equiv \mathrm{Tr}(U_i^2 \rho_{\rm B}) / 2k_{\rm B}T \tag{10}$$

and the reorganization energy for the  $|j\rangle$  to  $|n\rangle$  transition,

$$\lambda_{jn} \equiv \lambda_j + \lambda_n \,. \tag{11}$$

Using our Liouville space coupling scheme [11] we get

$$K_{31} = \frac{2V_{12}^2 V_{23}^2}{\hbar} \operatorname{Re} \int_0^\infty dt_1 \int_0^\infty dt_2 \int_0^\infty dt_3$$
  

$$\times \exp(-i\Delta E_{23}t_1 - i\Delta E_{13}t_2 - i\Delta E_{12}t_3)$$
  

$$\times \exp\{-k_{\rm B}T[\lambda_1(t_2 + t_3)^2 + \lambda_2(t_1 - t_3)^2 + \lambda_3(t_1 + t_2)^2]\}.$$
(12)

When the time integrations in eq. (12) are carried out, the superexchange rate is finally given by

$$K_{31} = \frac{2\pi}{\hbar} V_{12}^2 V_{23}^2 [R_{13}I(\eta_{13}) S_{13}(\Delta E_{13}) - R_{12}I(\eta_{12}) S_{12}(\Delta E_{12}) - R_{23}I(\eta_{23}) S_{23}(\Delta E_{23})].$$
(13)

Here

$$R_{jk} = \frac{\lambda_{jk}}{(\lambda_1 \lambda_2 + \lambda_1 \lambda_3 + \lambda_2 \lambda_3) 2k_{\rm B}T},$$
 (14a)

$$\eta_{jn} = \sqrt{R_{jn}} \, \frac{\Delta E_{jm} \lambda_n + \Delta E_{nm} \lambda_j}{\lambda_{jn}} \,, \tag{14b}$$

$$S_{jn}(x) = \frac{1}{\sqrt{4\pi k_{\rm B} T \lambda_{jn}}} \exp\left(-\frac{x^2}{4k_{\rm B} T \lambda_{jn}}\right), \qquad (14c)$$

where j, n, m are permutations of 1, 2, 3.  $S_{jn}(x)$  is just a Franck-Condon-weighted density of states. Using the definitions (9)-(11) we have

$$\Delta E_{12} = \Delta G_{12}^0 - \lambda_{12} , \qquad (15a)$$

$$\Delta E_{13} = \Delta G_{13}^0 - \lambda_{13} , \qquad (15b)$$

$$\Delta E_{23} = \Delta G_{23}^0 + \lambda_2 - \lambda_3 . \tag{15c}$$

Note that  $\Delta E_{jn} = -\Delta E_{nj}$ ,  $\Delta G_{jn}^0 = -\Delta G_{nj}^0$  and  $\lambda_{jn} = \lambda_{nj}$ . The function I(x) is given by

$$I(x) = -\int_{0}^{\infty} t \cos(xt) \exp(-t^{2}/2) dt.$$
 (16)

We have constructed the following Padé approximant, which provides a very good fit (better than 4%) for I(x):

$$I(x) \approx \frac{-1 + 0.5851x^2}{1 + 0.4149x^2 + 0.1235x^4},$$
  

$$|x| < 2.1,$$
  

$$\approx \frac{-1 + 0.5994x^2}{11.2551 - 3.8396x^2 + 0.5994x^4},$$
  

$$|x| \ge 2.1.$$
(17a)

Note the following limiting behavior of I(x):

$$I(x) = \frac{1}{x^2}, \qquad x \gg 1,$$
  
=  $-1 + \frac{1}{2}x^2, \quad x \ll 1.$  (17b)

The general expression of the reverse rate  $K_{13}$  can be obtained from (13) and (14) by replacing the vertical transition energies  $\Delta E_{13}$ ,  $\Delta E_{23}$  and  $\Delta E_{12}$  by  $\Delta G_{13}^0 + \lambda_{13}$ ,  $\Delta G_{23}^0 + \lambda_{23}$  and  $\Delta G_{12}^0 + \lambda_1 - \lambda_2$ , respectively. Eqs. (13) and (14) which hold for any value of the energy parameters are the main result of this paper. The fluctuations in the energy levels  $|1\rangle$ ,  $|2\rangle$ and  $|3\rangle$  are fully incorporated in this theory and this is why it holds for arbitrary values of  $\Delta G_{in}^0$  and  $\lambda_{in}$ . In contrast, the simple superexchange matrix element (eq. (2)) depends only on the average over the fluctuations and consequently it breaks down when  $\Delta G_{12}^0 - \lambda_{12}$  vanishes. It should be noted that for certain values of the parameters,  $K_{31}$  (eq. (13)) can become negative. This may happen when  $\Delta E_{13} \gg \sqrt{k_{\rm B}T\lambda_{13}}$  and level  $E_2$  is located between  $E_1$ and  $E_3$ . In this case the system cannot be described by simple rate equations and one should calculate the frequency-dependent rate  $K_{31}(s)$  which enters in a generalized rate equation (with a memory) [11]. Our  $K_{31}$  is then equal to the zero frequency value of the generalized rate  $K_{31}(s=0)$ . For the subsequent discussion we recall that the nonadiabatic rates  $K_{21}$ 

and  $K_{32}$  are given within the same approximation by [5]

$$K_{21} = \frac{2\pi}{\hbar} |V_{12}|^2 S_{12} (\Delta G_{12}^0 - \lambda_{12}) , \qquad (18a)$$

$$K_{32} = \frac{2\pi}{\hbar} |V_{23}|^2 S_{23}(\Delta G_{23}^0 - \lambda_{23}) .$$
 (18b)

We shall now examine a few limiting cases of eq. (13). We first consider the case where the energy level  $|2\rangle$  is sufficiently far from the energy levels  $|1\rangle$  and  $|3\rangle$ , i.e.

$$\Delta E_{12} \gg \sqrt{\lambda_{12} k_{\rm B} T}, \quad \Delta E_{23} \gg \sqrt{\lambda_{23} k_{\rm B} T} . \tag{19}$$

Condition (19) implies that the activation energies  $\Delta G_{12}^* \equiv (\Delta G_{12}^0 - \lambda_{12})^2 / 4\lambda_{12}$  and  $\Delta G_{23}^* \equiv (\Delta G_{23}^0 + \lambda_2 - \lambda_3)^2 / 4\lambda_{23}$  are much larger than  $k_{\rm B}T$ . This limit is where the conventional superexchange theory is usually formulated [3,4,14,15]. In this case eq. (13) assumes the form

$$K_{31} = \frac{2\pi}{\hbar} |V_{\rm SE}|^2 S_{13}(\Delta E_{13}), \qquad (20a)$$

with

$$V_{\rm SE} = \frac{V_{12}V_{23}}{\Delta E_{12}(\lambda_3/\lambda_{13}) + \Delta E_{32}(\lambda_1/\lambda_{13})} \,. \tag{20b}$$

Eqs. (20) reduce to the ordinary superexchange rate (1) and (2) when the electron transfer process is activationless, i.e.  $\Delta E_{13} = 0$ , so that  $\Delta E_{12} = \Delta E_{32}$ . In this limit  $K_{31}$  and the reverse rate  $K_{13}$  satisfy the detailed-balance condition

$$\frac{K_{13}}{K_{31}} = \exp\left(-\frac{\Delta G_{13}^0}{k_{\rm B}T}\right).$$
 (21)

We next consider another limiting case where all three states are completely degenerate, i.e.  $\Delta E_{12} = \Delta E_{23}$  $= \Delta E_{13} = 0$ . We further assume  $\lambda_1 = \lambda_2 = \lambda_3 \equiv \lambda$ . We then obtain from eq. (13)

$$K_{31} = \frac{2\pi}{\hbar} |V_{\rm SE}|^2 S_{13}(0) , \qquad (22a)$$

where

$$V_{\rm SE} = \frac{V_{12} V_{23}}{\sqrt{3\lambda k_{\rm B} T}}.$$
 (22b)

Eqs. (22) may be rationalized using a simple phys-414 ical argument. The variance of the energy level fluctuations is  $\approx \sqrt{\lambda k_{\rm B}T}$ .  $V_{\rm SE}$  is thus given by  $V_{12}V_{23}$  divided by a typical energy fluctuation.

#### 3. Application to the photosynthetic reaction center

We have calculated  $K_{31}$  using eq. (13) and the results are displayed as a function of  $\Delta E_{21} = \Delta G_{21}^0 + \lambda_{12}$  for different activation energies  $\Delta E_{13}$  (fig. 3a)



Fig. 3 (a) The dependence of the superexchange rate  $K_{31}$  on  $\Delta E_{21}$ for different values of  $\Delta E_{13}$ . Curves a, b and c correspond to  $\Delta E_{13}=0$ , 400 and 700 cm<sup>-1</sup>, respectively. The other parameters in this calculation are:  $\lambda_{12}=1000$  cm<sup>-1</sup>,  $\lambda_{23}=1500$  cm<sup>-1</sup>,  $\lambda_{13}=2000$  cm<sup>-1</sup>,  $V_{12}=80$  cm<sup>-1</sup>,  $V_{23}=6V_{12}$ , T=300 K. The dashed line represents the conventional superexchange rate (eqs. (20)) with  $\Delta E_{13}=0$ . (b) The superexchange rate  $K_{31}$  versus  $\Delta E_{21}$ for different values of the reorganization energy  $\lambda_{12}$ . Curves a, b and c correspond to  $\lambda_{12}=500$ , 1000 and 2500 cm<sup>-1</sup>,  $V_{12}=80$ cm<sup>-1</sup>,  $V_{23}=6V_{12}$ , T=300 K.

and reorganization energies  $\lambda_{12}$  (fig. 3b). The dashed line in fig. 4 represents the asymptotic rate expression (eqs. (20)). Fig. 3 also demonstrates that  $\Delta E_{13}$ and  $\lambda_{12}$  have a strong effect on the rate  $K_{31}$  for small values of  $\Delta E_{21}$  and have a negligible effect for large values of  $\Delta E_{21}$ , where the asymptotic rate expression (eqs. (20)) holds. Assuming that  $K_{32} \gg K_{21}$ , as sug-



Fig. 4. (a) The relative contribution of the superexchange mechanism R versus  $\Delta E_{21}$  for different values of the reorganization energy  $\lambda_{12}$ . Curves a, b and c correspond to  $\lambda_{12} = 100$ , 500 and 1000 cm<sup>-1</sup>, respectively. The other parameters are:  $\lambda_{13} = 2000$  cm<sup>-1</sup>,  $\lambda_{23} = 2000$  cm<sup>-1</sup>,  $V_{12} = 80$  cm<sup>-1</sup>,  $V_{23} = 6V_{12}$ , T = 300 K. (b) The minimum coupling  $V_{12}^{min}$  (solid line) and the corresponding minimum energy  $\Delta E_{21}^{min}$  (dashed line) required for the superexchange mechanisms to be dominant ( $R \ge 0.9$ ), are plotted versus  $\lambda_{12}$ . The other parameters are  $\lambda_{13} = 2000$  cm<sup>-1</sup>,  $\Delta E_{13} = 0$ ,  $V_{23} = 6V_{12}$ , T = 300 K.

gested by the ultrafast measurements [6,7], then the sequential rate is basically equal to  $K_{21}$ . The following dimensionless parameter,

$$R \equiv \frac{K_{31}}{K_{31} + K_{21}},\tag{23}$$

provides a measure of the relative contribution of the superexchange and the sequential mechanisms. R is bounded between 0 and 1.  $R \rightarrow 0$  when the sequential transfer dominates, and  $R \rightarrow 1$  when the superexchange transfer dominates. Fig. 4a displays the dependence of R on the energy  $\Delta E_{21}$  for different values of  $\lambda_{12}$ . Estimates of the various parameters in the RC vary considerably among authors [2]. In the following discussion we shall use the parameters  $V_{23}/$  $V_{12} = 6$ ,  $\Delta E_{13} = 0$ ,  $\lambda_{13} = 2000$  cm<sup>-1</sup>. We further recall that the rise rate of level  $|3\rangle$  following the preparation of level  $|1\rangle$  is  $3.6 \times 10^{11}$  s<sup>-1</sup>. If the superexchange mechanism is dominant this should be the value of  $K_{31}$ . We have varied  $\Delta E_{21}$ ,  $\lambda_{12}$ ,  $\lambda_{23}$  and  $V_{12}$ and searched for ranges of parameters for which the superexchange mechanism is dominant, defined as  $R \ge 0.9$ . It is clear that in order to reproduce the experimental rise-time of level  $|3\rangle$ ,  $V_{12}$  has to be larger than some minimum value  $V_{12}^{\min}$  which depends on the other parameters. We found that  $\lambda_{23}$  has little effect on  $V_{12}^{\min}$ , changing it by less than 2 cm<sup>-1</sup> as  $\lambda_{23}$ varies from 1500 to 3000  $cm^{-1}$ . Fig. 4b displays  $V_{12}^{\min}$  (solid line) plotted against  $\lambda_{12}$ . For each value of  $V_{12}^{\min}$ , the superexchange mechanism will be dominant if  $\Delta E_{21}$  is large enough. We have defined  $\Delta E_{21}^{\min}$  to be the value of  $\Delta E_{21}$  for which R = 0.9, for a given  $\lambda_{12}$  and  $V_{12}^{\min}$ . For  $\Delta E_{21} \ge \Delta E_{21}^{\min}$  the superexchange mechanism is dominant,  $\Delta E_{21}^{\min}$  is also displayed in fig. 4b (dashed line). We conclude from fig. 4b that in order for the superexchange mechanisms to be dominant, the coupling constant  $V_{12}$  must be larger than 73  $cm^{-1}$ .

Our rate expression (eq. (13)) was obtained in the high temperature limit. In order to extend it to low temperatures we need to adopt a more specific model for  $H_B$  and  $U_j$ . A common model in electron transfer theories assumes that  $U_j$  is proportional to a simple harmonic coordinate representing an intramolecular or intermolecular vibration. In this case eqs. (13) should be modified by replacing all  $k_BT$ factors by the average oscillator energy  $\langle \epsilon \rangle$  [7,16]

$$\langle \epsilon \rangle = \frac{1}{2} \hbar \omega \coth\left(\frac{\hbar \omega}{2k_{\rm B}T}\right).$$
 (24)

Note that in the high temperature  $(k_{\rm B}T \gg \hbar\omega)$  limit  $\langle \epsilon \rangle = k_{\rm B}T$ . When  $k_{\rm B}T$  in eq. (13) is replaced by  $\langle \epsilon \rangle$  (eq. (24)) we obtain a rate expression which is not restricted to the high temperature limit. Martin et al. [7] have measured the temperature dependence of the RC electron transfer in the range 10 to 300 K. For *Rb. sphaeroides* the variation of the rate was found to be in agreement with the conventional superexchange rate assuming a single mode with  $\omega = 80$  cm<sup>-1</sup>. For *Rps. virides* on the other hand the conventional expression is inadequate and the best fit obtained [7] (using  $\omega = 25$  cm<sup>-1</sup>) is shown in fig. 5 (dashed line). Fig. 5 also shows the temperature dependence of our new expression for  $K_{31}$  (eq. (13) together with eq. (24)). It is clear that our expression



Fig. 5. Temperature dependence of the superexchange rate  $K_{31}$ . A coupling to a single vibrational mode with  $\omega = 90 \text{ cm}^{-1}$  is assumed and the calculation used eq. (13) with  $k_{\rm B}T$  replaced by  $\langle \epsilon \rangle$  (eq. (24)). Curves a, b and c correspond to  $\Delta E_{21} = 800 \text{ cm}^{-1}$ ,  $\Delta E_{21} = 1050 \text{ cm}^{-1}$  and  $\Delta E_{21} = 1500 \text{ cm}^{-1}$ , respectively. The dashed curve represents the best fit with the conventional super-exchange rate using  $\omega = 25 \text{ cm}^{-1}$  (eq. (2) in ref. [7]). The points (+) show the experimental electron transfer rate in *Rps. viridis* from Martin et al. [7]. Other parameters in this calculation are  $\lambda_{13} = 2000 \text{ cm}^{-1}$ ,  $\lambda_{12} = 200 \text{ cm}^{-1}$ ,  $\lambda_{23} = 2000 \text{ cm}^{-1}$ ,  $V_{12} = 79 \text{ cm}^{-1}$ ,  $V_{23} = 6V_{12}$ ,  $\Delta E_{13} = 0$ . This figure shows that our superexchange expression (curve b) provides a better fit with experiment than the conventional super-exchange expression (dashed curve).

sion is in better agreement with experiment than the ordinary superexchange rate.

#### Acknowledgement

The support of the Office of Naval Research, the National Science Foundation and the Petroleum Research Fund, administered by the American Chemical Society, is gratefully acknowledged.

### References

- [1] J. Deisenhofer, O. Epp, M. Miki, R. Huber and H. Michel, Nature 318 (1985) 618.
- [2] J. Breton and A. Vermeglio, eds., The photosynthetic bacterial reaction center (Plenum Press, New York, 1988).
- [3] R.A. Marcus, Chem. Phys. Letters 133 (1987) 471; in: The photosynthetic bacterial reaction center, eds. J. Breton and A. Vermeglio (Plenum Press, New York, 1988) p. 389.
- [4] M. Bixon, J. Jortner, M. Plato and M.E. Michel-Beyerle, in: The photosynthetic bacterial reaction center, eds. J. Breton and A. Vermeglio (Plenum Press, New York, 1988) p. 399.
- [5] R.A. Marcus and N. Sutin, Biochim. Biophys. Acta 811 (1985) 265.
- [6] J. Breton, J.L. Martin, A. Migus, A. Antonetti and A. Orszag, Proc. Natl. Acad. Sci. US 83 (1986) 5121;
   G.R. Fleming, J.L. Martin and J. Breton, Nature 333 (1988) 190.
- [7] J.L. Martin, J. Breton, J.C. Lambry and G.R. Fleming, in: The photosynthetic bacterial reaction center, eds. J. Breton and A. Vermeglio (Plenum Press, New York, 1988) p. 195.
- [8] J.M. Hayes and G.S. Small, J. Phys. Chem. 90 (1986) 4928;
  S.R. Meech, A.J. Hoff and D.A. Wiersma, Chem. Phys. Letters 121 (1985) 287;
  S.J. Boxer, D.S. Gottfried, D.J. Lockhart and T.R. Midderdorf, J. Chem. Phys. 86 (1987) 2439.
- [9] Y. Won and R.A. Friesner, J. Phys. Chem. 92 (1988) 2214.
- [10] Y. Won and R.A. Friesner, Biochim. Biophys. Acta 935 (1988) 9.
- [11] M. Sparpaglione and S. Mukamel, J. Chem. Phys. 88 (1988) 5;

Y.J. Yan, M. Sparpaglione and S. Mukamel, J. Phys. Chem. 92 (1988) 4842.

- [12] J.S. Bader and D. Chandler, Chem. Phys. Letters 157 (1989) 501.
- [13] S. Mukamel, Advan. Chem. Phys. 70 (1988) 165.
- [14] R. Hoffmann, A. Inamura and W. Hehne, J. Chem. Soc. (1968) 1499;

E. Stein and H. Taube, J. Am. Chem. Soc. 103 (1981) 693.

[15] A. Beretan and J.J. Hopfield, J. Am. Chem. Soc. 106 (1984)
 1584;
 M. Redi and J.J. Hopfield, J. Chem. Phys. 72 (1980) 6651;

J.R. Miller and J.V. Beitz, J. Chem. Phys. 74 (1981) 6746.

[16] M. Bixon and J. Jortner, J. Phys. Chem. 90 (1986) 3795.